

Name: _____ Hour: _____ Date: _____

What was the real average for the Semester Exam?



How did the Semester Final go? Today, we will be taking a **sample** from a **population**. We will use the average from the **sample** to estimate the average for the **population**.

Yesterday we looked at a very small class of students as the population. In reality there were many students who took the test. (*The list of the scores is in the table below*)

Take a **random sample of 5 students** and record their scores. Then find the mean. Repeat this for a total of 4 times.

Scores: _____ Mean: _____ Scores: _____ Mean: _____

Scores: _____ Mean: _____ Scores: _____ Mean: _____

Semester Final Scores (plus extras)

| Student # | Score | Student # | Score | Student # | Score | Student # | Score | Student # | Score |
|------------|-------|------------|-------|------------|-------|------------|-------|------------|-------|
| Student 1 | 114 | Student 18 | 93 | Student 35 | 75 | Student 52 | 72 | Student 69 | 114 |
| Student 2 | 99 | Student 19 | 124 | Student 36 | 90 | Student 53 | 117 | Student 70 | 93 |
| Student 3 | 102 | Student 20 | 108 | Student 37 | 114 | Student 54 | 81 | Student 71 | 120 |
| Student 4 | 111 | Student 21 | 96 | Student 38 | 90 | Student 55 | 99 | Student 72 | 108 |
| Student 5 | 108 | Student 22 | 69 | Student 39 | 108 | Student 56 | 90 | Student 73 | 117 |
| Student 6 | 90 | Student 23 | 114 | Student 40 | 105 | Student 57 | 117 | Student 74 | 72 |
| Student 7 | 93 | Student 24 | 81 | Student 41 | 122 | Student 58 | 105 | Student 75 | 93 |
| Student 8 | 108 | Student 25 | 93 | Student 42 | 96 | Student 59 | 102 | Student 76 | 72 |
| Student 9 | 111 | Student 26 | 122 | Student 43 | 117 | Student 60 | 96 | Student 77 | 111 |
| Student 10 | 105 | Student 27 | 120 | Student 44 | 99 | Student 61 | 63 | Student 78 | 114 |
| Student 11 | 120 | Student 28 | 99 | Student 45 | 102 | Student 62 | 111 | Student 79 | 96 |
| Student 12 | 66 | Student 29 | 114 | Student 46 | 108 | Student 63 | 108 | Student 80 | 121 |
| Student 13 | 93 | Student 30 | 87 | Student 47 | 99 | Student 64 | 96 | Student 81 | 93 |
| Student 14 | 108 | Student 31 | 111 | Student 48 | 90 | Student 65 | 93 | Student 82 | 114 |
| Student 15 | 122 | Student 32 | 120 | Student 49 | 117 | Student 66 | 111 | Student 83 | 96 |
| Student 16 | 87 | Student 33 | 81 | Student 50 | 114 | Student 67 | 105 | Student 84 | 72 |
| Student 17 | 111 | Student 34 | 90 | Student 51 | 111 | Student 68 | 81 | Student 85 | 117 |

1. Write each mean on a different sticker and put the stickers in the appropriate location on the poster at the front of the room. Copy down the dotplot that is created on the poster.

2. What does each dot on the poster represent?

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3. What do you think the true Semester Final average is?
4. A **sampling distribution** shows the means calculated from all of the possible samples of size 5 from the population. Is the above dotplot a sampling distribution? Explain.
5. We took a random sample of 5 test scores at Male high school and got a mean of 80. What about 90? Is this **convincing evidence** that Male students did worse than students at our school or is it possible the Male has the same average?

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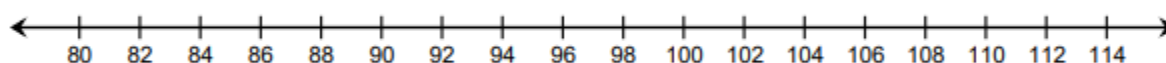
1 Random SAMPLE

Scores: 99,93,105, 90,111 Mean: $\bar{x} = 99.6$ Scores: _____ Mean: _____

Scores: _____ Mean: _____ Scores: _____ Mean: _____

1. Write each mean on a different sticker and put the stickers in the appropriate location on the poster at the front of the room. Copy down the dotplot that is created on the poster.

(insert class data for dot plot below)



Distribution of sample means (\bar{x})

2. What does each dot on the poster represent?

A random sample of 5 students and the mean of their exam scores, so each dot is a *statistic*!

3. What do you think the true Semester Final average is? (make a guess)
4. A **sampling distribution** shows the means calculated from all of the possible samples of size 5 from the population. Is the above dotplot a sampling distribution? Explain.

NO, this is a **distribution of many samples** of the same size ($n = 5$), but it does not represent every possible unique sample from this population ($N = 85$). To create the actual **sampling distribution** would necessitate taking every possible combination of score randomly selected scores, which would result in infinitely more unique samples.

$${}_{85}C_5 = \binom{85}{5} = 32,801,517$$

5. We took a random sample of 5 test scores at Male high school and got a mean of 80. Is this **convincing evidence** that Male students did worse than students at our school or is it possible the Male has the same average?

To be convincing evidence, we would want the probability of obtaining this sample mean to be small enough that we would not expect it to happen simply by chance, or to occur so rarely that it would be very unlikely to assume that the students at Male would have the same average as students from Manual based upon this sample statistic.

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What is a Sampling Distribution? Day 2

Important ideas: **Evaluating a claim**

Check Your Understanding

Pennies made prior to 1982 were made of 95% copper. Because of their copper content, these pennies are worth about \$0.023 each. Pennies made after 1982 are only 2.5% copper. Jenna reads online that 13.2% of pennies in circulation are pre-1982 copper pennies. Jenna has a large container of pennies at home. She selects a random sample of 50 pennies from the container and finds that 11 are pre-1982 copper pennies. Does this provide convincing evidence that the proportion of pennies in her container that are pre-1982 copper pennies is greater than 0.132?

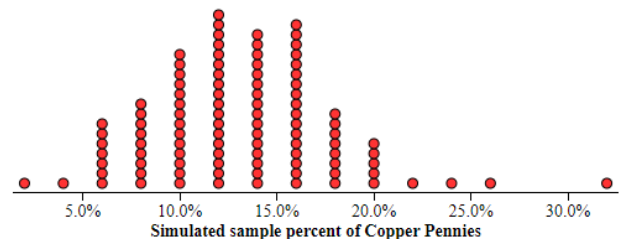
1. Identify the population, parameter, sample and statistic.

Population: _____ Parameter: _____

Sample: _____ Statistic: _____

2. Does Jenna have some evidence that more than 13.2% of her pennies are pre-1982 copper pennies?
3. Provide two explanations for the evidence described in #2.

We used technology to simulate selecting 100 SRSs of size $n = 50$ from a population of pennies in which 13.2% are pre-1982 copper pennies. The dotplot shows \hat{p} = the sample proportion of copper pennies for each of the 100 samples.



4. There is one dot on the graph at 0.22 (or 22%). Explain what this dot represents.
5. Assuming that 13.2% of pennies in circulation are pre-1982 copper pennies, is it surprising to randomly select 50 pennies for which $\hat{p} = 11/50 = 22\%$ or greater? Justify your answer.

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6. Based on your previous answers, is there convincing evidence that more than 13.2% of pennies in Jenna's container are pre-1982 copper pennies? Explain your reasoning.

What is a Sampling Distribution? Day 2

Important ideas:

[LT#1] Evaluating a Claim

- ① Assume the claim is true.
- ② Create simulated sampling distribution.
- ③ Find % chance of getting observed result.

Claim is true

% of dots

observed result

If $< 5\%$ → convincing evidence against claim.
 If $\geq 5\%$ → not convincing evidence against claim

Check Your Understanding

Pennies made prior to 1982 were made of 95% copper. Because of their copper content, these pennies are worth about \$0.023 each. Pennies made after 1982 are only 2.5% copper. Jenna reads online that 13.2% of pennies in circulation are pre-1982 copper pennies. Jenna has a large container of pennies at home. She selects a random sample of 50 pennies from the container and finds that 11 are pre-1982 copper pennies. Does this provide convincing evidence that the proportion of pennies in her container that are pre-1982 copper pennies is greater than 0.132?

1. Identify the population, parameter, sample and statistic.

Population: All pennies in container Parameter: $0.132 = p$

Sample: 50 pennies Statistic: $11/50 = 0.22 = \hat{p}$

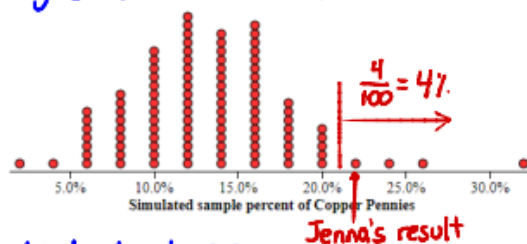
2. Does Jenna have some evidence that more than 13.2% of her pennies are pre-1982 copper pennies?

Yes, in her sample she had 22%, which is greater than 13.2%.

3. Provide two explanations for the evidence described in #2.

- ① The percent in the container is 13.2% and she got lucky in her sample.
- ② The percent in the container really is greater than 13.2%.

We used technology to simulate selecting 100 SRSs of size $n = 50$ from a population of pennies in which 13.2% are pre-1982 copper pennies. The dotplot shows \hat{p} = the sample proportion of copper pennies for each of the 100 samples.



4. There is one dot on the graph at 0.22 (or 22%). Explain what this dot represents.

One random sample of 50 pennies, which had 22% copper pennies.

5. Assuming that 13.2% of pennies in circulation are pre-1982 copper pennies, is it surprising to randomly select 50 pennies for which $\hat{p} = 11/50 = 22\%$ or greater? Justify your answer.

Yes, only 4 of the samples had 22% or greater. $\frac{4}{100} = 4\%$.

6. Based on your previous answers, is there convincing evidence that more than 13.2% of pennies in Jenna's container are pre-1982 copper pennies? Explain your reasoning.

Yes. Assuming Jenna's container had 13.2% copper pennies, it is unlikely (4%) to get a sample of 50 with 22% or greater.

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